

# On exceptional properties of $f$ -divergence minimal martingale measures for exponential Levy models

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## Abstract

We study such important properties of  $f$ -divergence minimal martingale measure as Levy preservation property, scaling property, invariance in time property for exponential Levy models. We give some useful decomposition for  $f$ -divergence minimal martingale measures and we answer on the question which form should have  $f$  to ensure mentioned properties. We show that  $f$  is not necessarily common  $f$ -divergence. For common  $f$ -divergences, i.e. functions verifying  $f''(x) = ax^\gamma$ ,  $a > 0$ ,  $\gamma \in \mathbb{R}$ , we give necessary and sufficient conditions for existence of  $f$ -divergence minimal martingale measure. As an application we give explicit formulas for utility maximising strategies of exponential Levy models.

KEY WORDS AND PHRASES:  $f$ -divergence, exponential Levy models, minimal martingale measures, Levy preservation property

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