

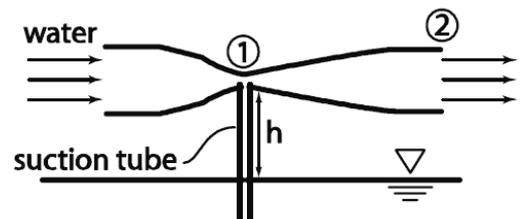
Below, five (5) questions are given, hand in answers for only (i.e. not more than) four (4) questions. Choose as you wish. The four questions give max 30 points = $7\frac{1}{2} + 7\frac{1}{2} + 7\frac{1}{2} + 7\frac{1}{2}$ points. The total score then gives the final result according to ≥ 13 p. = 1; $\geq 16\frac{1}{2}$ p. = 2; ≥ 20 p. = 3; $\geq 23\frac{1}{2}$ p. = 4; ≥ 27 p. = 5. The amount of credits for this course is 4 sp.

All support material is allowed except for telecommunication devices and personal help including computers.

In all questions, use for ambient conditions temperature $T^\circ = 293$ K, $p^\circ = 1$ bar = 10^5 Pa if not stated otherwise.

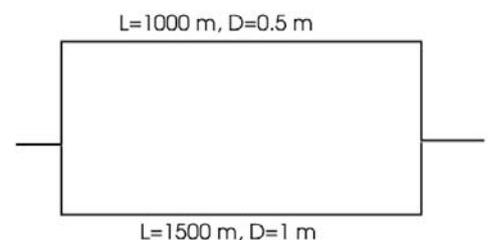
0. Did you already give your course evaluation för this course via the webpage http://web.abo.fi/fak/ktf/vt/Eng/education_Evaluation.htm or shall you soon do this?

011. The figure shows a fertilizer sprayer that uses a Venturi nozzle. Water (density $\rho = 1000$ kg/m³) moving through this nozzle reaches a low pressure at section ①. This low pressure draws liquid fertilizer (assume that the fertilizer has the properties of water) up the suction tube, and the mixture is jetted to the ambient surroundings ($p_2 = p^\circ = 100$ kPa) at section ②. Nozzle dimensions are $d_1 = 3$ mm at ①, $d_2 = 9$ mm at ②, and $h = 150$ mm.

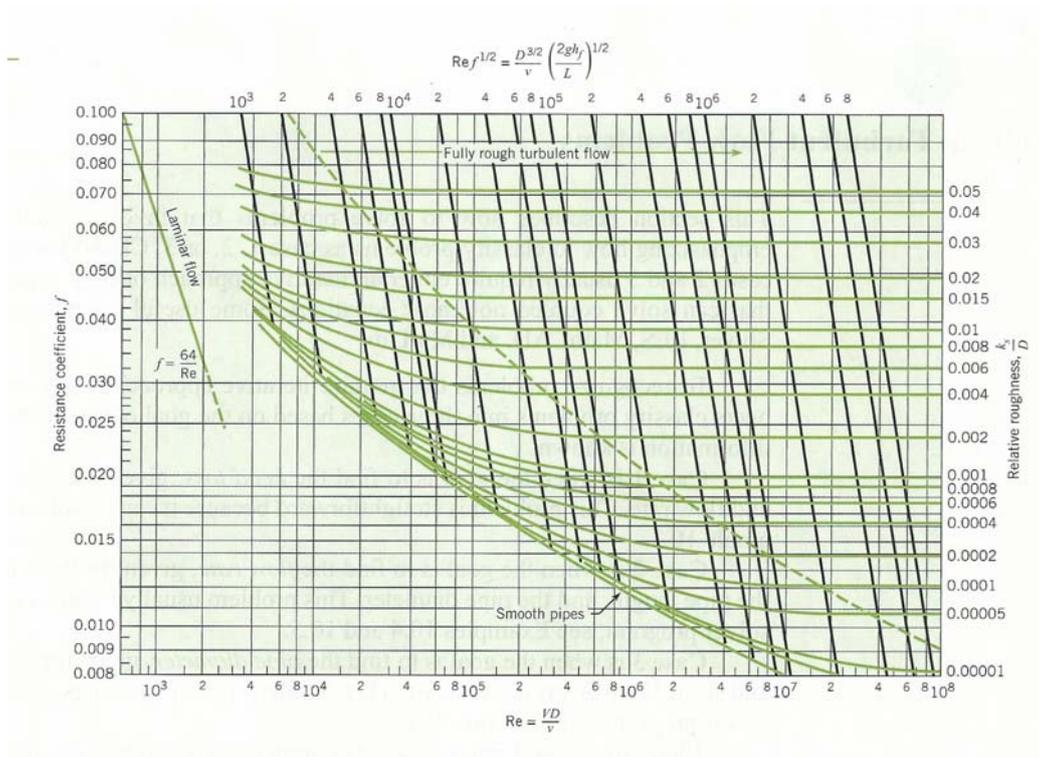


- a) Determine the minimum possible water speed (v_2) at the exit of the nozzle so that fluid will be drawn up the suction tube. (Bernoulli's equation applies to expansion ① \rightarrow ②). (6 p.)
b) Repeat the calculation for a) if the density of the fertilizer liquid $\rho_F = 1100$ kg/m³. (1½ p.)

012. A piping system consists of two parallel pipes as shown in the diagram. One pipe has an internal diameter of $D_1 = 0.5$ m and is $L_1 = 1000$ m long. The other pipe has an internal diameter of $D_2 = 1$ m and is $L_2 = 1500$ m long. Both pipes are made of cast iron (wall roughness $k = 0,26$ mm). The pipes are transporting water at 20°C (density $\rho = 1000$ kg/m³, kinematic viscosity $\nu = 10^{-6}$ m²/s). The total flow rate is 4 m³/s. There is no elevation change (the system is horizontal). Neglect minor losses.



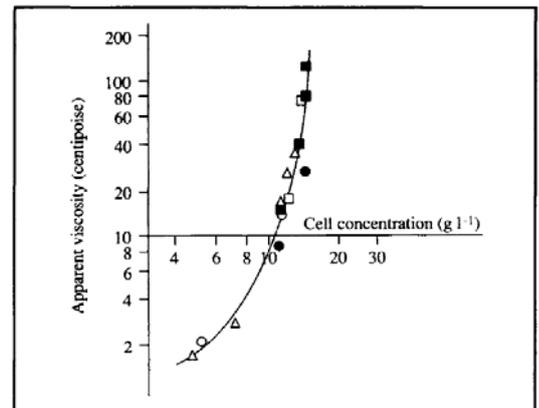
- a) Show that the ratio of the velocities V_2/V_1 is given by $V_2/V_1 = A \cdot \sqrt{(\zeta_1/\zeta_2)}$ and give the value for constant A. (1½ p.)
b) Show that a mass balance gives 4 m³/s = $V_1 \cdot (B + C \cdot \sqrt{(\zeta_1/\zeta_2)})$ and give the values for constants B and C. (1½ p.)
c) Find the flow rate in each pipe and the pressure drop in the system. (4½ p.)
See the Moody diagram on the next page for determining the friction coefficients ζ ; start iterations with assuming Fully rough turbulent flow. (Note: in this diagram $\zeta =$ symbol f).



013. The figure → gives the relation between the dynamic viscosity η (1 centipoise = 0,001 Pa·s) of various plant cell suspensions in water as function of their concentration c (in g/l = kg/m³).

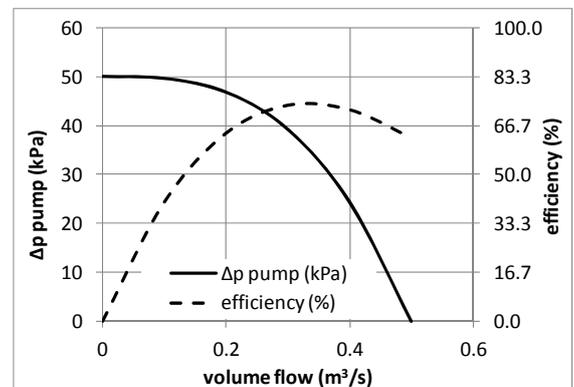
In a (bio-)process the concentration of plant material in a water stream increases from 5 g/l to 15 g/l.

A pump system is designed to transport a flow $Q = 0.2$ m³/s out of the system and transport it over a distance of $L = 50$ m through a smooth (plastic) pipe with $D = 20.3$ cm inside diameter.



For the density of the suspension it may be assumed that it is ~ constant at 1000 kg/m³; for water $\eta = 0,001$ Pa·s. A Moody diagram for determining the tube flow friction coefficient is given above on this page. (Note: in this diagram $\zeta = \text{symbol } f$).

- Calculate the theoretical pumping power needed to transport the starting (5 g/l) and final (15 g/l) suspensions. (2½ p.)
- Given a set of identical pumps with characteristics in the figure →, draw up a network with one or more of these pumps, plus valves, that allows for the transport of the suspensions, and allowing for the starting and final suspension concentrations. (2½ p.)
- What is the electric power consumption of the pump(s) system when operating at 5 g/l and at 15 g/l cell concentration, respectively. (2½ p.)



The pump characteristic is given by $\Delta p = 50 \cdot (1 - (Q/0,5)^3)$ kPa, for flow Q (m³/s).

014. A process slurry contains a solid particle concentration of $c_{in} = 3\%$ -vol in an aqueous flow of $2\text{ m}^3/\text{min}$. A continuous thickener is to be designed that concentrates the slurry to $c_{out} = 17\%$ -vol.

c %-vol	u cm/h
2	29
4	16.2
6	10.1
8	7.5
10	5
12	2.7
14	1.4
16	0.75
18	0.45
20	0.2

A series of batch settling tests was carried out with slurries of different concentrations of the same solid material, in water; the results of the measured settling velocity u is given in the table \rightarrow .

If needed, assume $\rho_s = 2650\text{ kg/m}^3$ for the density of the solid material; for water $\rho = 1000\text{ kg/m}^3$.

- Give an estimate for the sedimentation area for the continuous settler and, assuming a circular geometry, the diameter. Note: use only data from the table that is relevant! (6 p).
- Explain why (or show that) it is not necessary to assume a value for the density of the solid, making the calculation based on volumes to produce a result similar to under a). (1½ p).

015. A company that processes ore materials wishes to separate a mixture of two different minerals using a water – fluidised bed.

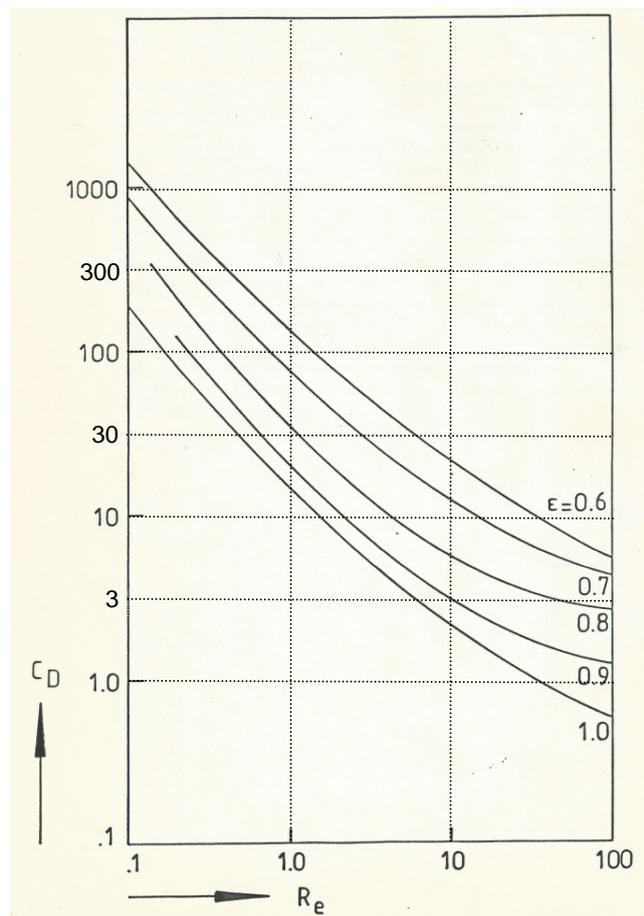
The two minerals “A” and “B” have the following (average) particle diameter d and solid density ρ_s :

A: $d = 100\ \mu\text{m}$; $\rho_s = 2750\text{ kg/m}^3$

B: $d = 120\ \mu\text{m}$; $\rho_s = 2500\text{ kg/m}^3$.

The density and dynamic viscosity of water are $\rho_l = 1000\text{ kg/m}^3$ and $\eta = 0,001\text{ Pa}\cdot\text{s}$.

The figure \rightarrow gives the relation between the particle Reynolds number Re (-), the drag coefficient C_D (-) for a single particle in the bed and the bed porosity (or voidage) ϵ (-). Assume spherical particles.



In the fluidized bed the minerals will form two layers.

- Determine which of the two minerals “A” and “B” will form the lower layer if the superficial velocity of the water is 0.8 cm/s . (Or: which of the two will give the highest effective density?) (5½ p.)
- Can this be reversed by increasing, or by decreasing the water flow velocity? (2 p.)